

## ECON 7331 — ECONOMETRICS I

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**Hours:** You can usually drop by anytime, sometimes I am out Thursday-Friday and sometimes I work at home in the morning, so email for an appointment if you want to be sure (emailing about appointments is the best way, because I use my inbox to keep track of appointments).

### **Obligatory Notices:**

Mental Health and Wellness Resources

The University of Houston has a number of resources to support students mental health and overall wellness, including CoogsCARE and the UH Go App. UH Counseling and Psychological Services (CAPS) offers 24/7 mental health support for all students, addressing various concerns like stress, college adjustment and sadness. CAPS provides individual and couples counseling, group therapy, workshops and connections to other support services on and off-campus. For assistance visit [uh.edu/caps](http://uh.edu/caps), call 713-743-5454, or visit a Lets Talk location in-person or virtually. Lets Talk are daily, informal confidential consultations with CAPS therapists where no appointment or paperwork is needed. The Student Health Center offers a Psychiatry Clinic for enrolled UH students. Call 713-743-5149 during clinic hours, Monday through Friday 8 a.m. - 4:30 p.m. to schedule an appointment. The A.D. Bruce Religion Center offers spiritual support and a variety of programs centered on well-being.

Need Support Now?

If you or someone you know is struggling or in crisis, help is available. Call CAPS crisis support 24/7 at 713-743-5454, or the National Suicide and Crisis Lifeline: call or text 988, or chat [988lifeline.org](https://988lifeline.org).

### Academic Honesty Policy

High ethical standards are critical to the integrity of any institution, and bear directly on the ultimate value of conferred degrees. All UH community members are expected to contribute to an atmosphere of the highest possible ethical standards. Maintaining such an atmosphere requires that any instances of academic dishonesty be recognized and addressed. The UH Academic Honesty Policy is designed to handle those instances with fairness to all parties involved: the students, the instructors, and the University itself. All students and faculty of the University of Houston are responsible for being familiar with this policy.

Title IX/Sexual Misconduct Per the UHS Sexual Misconduct Policy, your instructor is a responsible employee for reporting purposes under Title IX regulations and state law and must report incidents of sexual misconduct (sexual harassment, non-consensual sexual contact, sexual assault, sexual exploitation, sexual intimidation, intimate partner violence, or stalking) about which they

become aware to the Title IX office. Please know there are places on campus where you can make a report in confidence. You can find more information about resources on the Title IX website at <https://uh.edu/equal-opportunity/title-ix-sexual-misconduct/resources/>.

#### Reasonable Academic Adjustments/Auxiliary Aids

The University of Houston is committed to providing an academic environment and educational programs that are accessible for its students. Any student with a disability who is experiencing barriers to learning, assessment or participation is encouraged to contact the Justin Dart, Jr. Student Accessibility Center (Dart Center) to learn more about academic accommodations and support that may be available to them. Students seeking academic accommodations will need to register with the Dart Center as soon as possible to ensure timely implementation of approved accommodations. Please contact the Dart Center by visiting the website: <https://uh.edu/accessibility/> calling (713) 743-5400, or emailing [jdcenter@Central.UH.EDU](mailto:jdcenter@Central.UH.EDU).

#### Excused Absence Policy

Regular class attendance, participation, and engagement in coursework are important contributors to student success. Absences may be excused as provided in the University of Houston Undergraduate Excused Absence Policy and Graduate Excused Absence Policy for reasons including: medical illness of student or close relative, death of a close family member, legal or government proceeding that a student is obligated to attend, recognized professional and educational activities where the student is presenting, and University-sponsored activity or athletic competition. Under these policies, students with excused absences will be provided with an opportunity to make up any quiz, exam or other work that contributes to the course grade or a satisfactory alternative. Please read the full policy for details regarding reasons for excused absences, the approval process, and extended absences. Additional policies address absences related to military service, religious holy days, pregnancy and related conditions, and disability.

#### Recording of Class

Students may not record all or part of class, livestream all or part of class, or make/distribute screen captures, without advanced written consent of the instructor. If you have or think you may have a disability such that you need to record class-related activities, please contact the Justin Dart, Jr. Student Accessibility Center. If you have an accommodation to record class-related activities, those recordings may not be shared with any other student, whether in this course or not, or with any other person or on any other platform. Classes may be recorded by the instructor. Students may use instructors recordings for their own studying and notetaking. Instructors recordings are not authorized to be shared with anyone without the prior written approval of the instructor. Failure to comply with requirements regarding recordings will result in a disciplinary referral to the Dean of Students Office and may result in disciplinary action.

#### Recommended Language and Guidance

##### Resources for Online Learning

The University of Houston is committed to student success, and provides information to optimize the online learning experience through our Power-On website. Please visit this website for a com-

prehensive set of resources, tools, and tips including: obtaining access to the internet, AccessUH, Blackboard, and Canvas; using your smartphone as a webcam; and downloading Microsoft Office 365 at no cost. For questions or assistance contact UHOnline@uh.edu.

#### UH Email

Please check and use your CougarNet email for communications related to this course. Faculty use the CougarNet email to respond to course-related inquiries such as grade queries or progress reports for reasons of FERPA. To access your CougarNet email, login to your Microsoft 365 account with your CougarNet credentials. Visit University Information Technology (UIT) for instructions on how to connect your CougarNet e-mail on a mobile device. Webcams

Access to a webcam is required for students participating remotely in this course. Webcams must be turned on (state when webcams are required to be on and the academic basis for requiring them to be on). (Example: Webcams must be turned on during exams to ensure the academic integrity of exam administration.)

Security Escorts and Cougar Ride UHPD continually works with the University community to make the campus a safe place to learn, work, and live. The security escort service is designed for the community members who have safety concerns and would like to have a Security Officer walk with them, for their safety, as they make their way across campus. Based on availability either a UHPD Security Officer or Police Officer will escort students, faculty, and staff to locations beginning and ending on campus. If you feel that you need a Security Officer to walk with you for your safety, please call 713-743-3333. Arrangements may be made for special needs.

Parking and Transportation Services also offers a late-night, on-demand shuttle service called Cougar Ride that provides rides to and from all on-campus shuttle stops, as well as the MD Anderson Library, Cougar Village/Moody Towers and the UH Technology Bridge. Rides can be requested through the UH Go app. Days and hours of operation can be found at <https://uh.edu/af-university-services/parking/cougar-ride/>.

#### Syllabus Changes

Please note that the instructor may need to make modifications to the course syllabus. Notice of such changes will be announced as quickly as possible through (specify how students will be notified of changes).

#### Additional Recommended Issues to Address in the Syllabus

##### Artificial Intelligence

Instructors are recommended to develop language that will guide students in their use or prohibition of use of AI related tools. If an instructor allows the use of AI tools, they should clearly indicate in what ways they can be used, how they should be cited/reported, and for which assignments they are allowed. Note that Turnitin currently has a filter for ChatGPT, although there is approximately 2% rate of false positives. The following is a collection of classroom policies from a variety of universities for AI generative tools: Classroom Policies for AI Generative Tools (google.com).

### Online Exams

The Office of the General Counsel has recommended to make sure students are aware that: (1) students are permitted to take their online tests or quizzes in a computer lab or other open space; and (2) there is no requirement that a student use their own personal computer or that they complete exams and quizzes in any specific location (e.g., their home). The Office of the General Counsel has advised that students be made aware in advance that an environmental scan may be conducted as a part of an online exam.

### Learning Outcomes:

- Students will learn, through lectures, homeworks, and TA-sessions, to master econometric tools at a level that, in conjunction with other core-classes, enables the students to perform statistical analysis of economic models.
- Students will develop their technical skills as a background for doing empirical work to the level expected in graduate economics programs. For this purpose, student will learn to use the econometric software to estimate models on actual economic data.
- Students will learn the basic ideas of advanced econometrics with a focus on empirically relevant issues.

### Course Description

The topics you should know for the exam is what is taught in class. It is usually not helpful to read further material at this stage, but it is often very helpful to read an alternative presentation of the same material. Even undergraduate texts, which do not use matrix algebra, may be helpful in getting a better feeling for various tools.

#### Readings:

##### *Textbooks:*

I plan to use Hansen: “Econometrics” and some notes. In the past, I have used (and liked) Davidson and MacKinnon: “Econometric Theory and Methods” Oxford University Press 2004 and Econometric Analysis, William H. Greene, 7th Edition, Prentice Hall, 2012 (this book is among the 100 all-time most cited books in the world according to Prof. Greene’s web-site). I tend to think Greene is too long-winded, but maybe you like it. The based Econometrics I material is the same everywhere. But, again, you are supposed to know all that has been taught in class and nothing more.

*Notes* Notes, homeworks, information, etc. will be posted on the class web-page. The class web-page will be accessible from my home page.

Material covered last year (this is all standard stuff and this will be covered again—we may cover a little more or less. Some of the material near the end are given a more introductory treatment and we will return to it in Econometrics II:

1. Matrix algebra. There are good introductions to this material in Davidson-MacKinnon and Greene (I like Greene's appendices better on this). I list some of the more important stuff below (although it is not exhaustive). If you are not too familiar with matrix algebra, you may want to get an undergraduate book or do a little study group. But do something about it.
  - (a) You are expected to know the basic rules about adding and multiplying etc. matrices before taking this class.
  - (b) Partitioned matrices are important in econometrics, so you have to be able to invert and multiply those.
  - (c) A special case of writing a matrix in partitioned form is to write it as a collection of row vectors or a collection of column vectors. For the important issue of consistency of OLS, this is crucial.
  - (d) You are expected to be able to find the determinant of a  $2 \times 2$  matrix and matrices that are block-diagonal with  $2 \times 2$  matrices or scalars along the diagonal.
  - (e) You have to be able to diagonalize a symmetric matrix and you should know the role of the eigenvalues (More often, though, you will need to make a theoretical argument relying on the existence of a diagonalization, as opposed to doing it numerically). You should be able to find eigenvalue for  $2 \times 2$  matrices. This includes the taking of the square root of a matrix and the square root of the inverse.
  - (f) You should know about idempotent matrices and their eigenvalues (0 or 1).
2. Statistics
  - (a) You should know the multivariate normal distribution and how it relates to the  $\chi$ -square distribution.
  - (b) You have to be comfortable taking means and variances of a stochastic vector (a vector of stochastic variables).
  - (c) You should (absolutely) know what happens to the mean and variance of a stochastic vector if it is multiplied by a matrix.
  - (d) You should be able to explain why  $e'Me$  follows a  $\chi$ -square distribution if  $M$  is idempotent and  $e$  is standard normal (and explain the degrees of freedom).
  - (e) You have to know (for testing) that if  $X$  is  $N(0, \Sigma)$  then  $X'\Sigma^{-1}X$  is  $\chi$ -square. This follows because  $\Sigma^{-.5}X$  is  $N(0, I)$ , you should be able to explain this, but the higher priority is to know the result for  $X'\Sigma^{-1}X$  which is the multivariate equivalent of dividing by the standard error (if  $X$  is a scalar, then  $X'\Sigma^{-1}X$  is  $X^2/\sigma^2 = (X/\sigma)^2$ , i.e., the square of standard normal).
3. Theoretical derivation of the regression coefficient (vector) and its variance.
4. Be able to show the  $\hat{\beta}$  (the estimated coefficient in the linear regression model under the standard assumptions [know what those are]) is unbiased. The unbiased estimator of the error variance (be able to prove that it is unbiased).

5. Working with numerical examples—the linear model with 2 regressors will often be used in midterm/exam questions, I may give you some numbers and you should be able to find, say the coefficient and the standard errors.
6. The Frisch-Waugh (FM) theorem and applications. I may ask you to prove the FW theorem, so make sure you are comfortable working with the projection matrix  $P_X = X(X'X)^{-1}X'$  and the residual maker  $M_X = I - P_X = I - X(X'X)^{-1}X'$  Important applications of the FM theorem are
  - (a) Regressing on a large number of dummy variables.
  - (b) Showing the bias in the case of omitted (left-out) variables.
  - (c) Evaluating the marginal impact of an extra regressor.
  - (d) “Added value plots” (to check for outliers).
7.  $R^2$ , adjusted  $R^2$ , and partial  $R^2$
8. The t- and F-test (know how to formulate the test of hypothesis described in words and know the equivalence of the “goodness of fit” version and the version where you directly use  $R\hat{\beta} - q$  know how to prove that the F- and t-tests follow the t- and F-distributions). The Chow-test (and similar simple applications of the F-test that I may think of). Confidence intervals.
9. Functional Form (as I covered it in class: dummy variables, interactions, elasticities, semi-log, etc.)
10. Data issues: Classical measurement error, multi-collinearity
11. Asymptotics. You will need to use the Law of Large Numbers (LLN) and the Central Limit Theorem (CLT), but I did not mention the explicit version of the LLN or the CLT, so you can talk about “the” LLN, and “the” CLT.
  - (a) Consistency of the OLS estimator (know the assumptions needed on  $X'X$  and be able to explain that  $X'\epsilon$  is a sum of independent variables so that a LNN holds).
  - (b) Consistency of the variance estimator.
  - (c) Convergence of the  $t$ -test to a Normal test (whether the data are Normally distributed or not, as long a CLT holds).
  - (d) Asymptotic  $\chi^2$ -test of restrictions even if the errors are not Normally distributed (the case where they are, is of course a special case, so this implies that the standard F-test converges to the  $\chi^2$ -test (and the F-distribution to the  $\chi^2$ -distribution).
12. GLS. Understand that if  $\Omega$  is the variance matrix, one can choose a Cholesky factorization so that  $\Omega^{-1/2}$  is lower triangular and multiplying the  $n'$ th row with the true error vector corresponds to calculating  $x_n - E(x_n|x_{n-1}, \dots, x_1)$  (and scaling with the standard error). (Confer point 2e.) Therefore the elements of  $\Omega^{-1/2}e$  are i.i.d., which is equivalent to  $\text{var}(\Omega^{-1/2}e) = \Omega^{-1/2} \text{var}(e) \Omega^{-1/2'} = \Omega^{-1/2} \Omega \Omega^{-1/2'} = I$ . This got a little detailed, but you

can take that as a reminder that formulas for the variance of matrix times a stochastic vector are essential for OLS/GLS theory.

13. Feasible GLS. Main examples: 1) autocorrelation in residuals 2) heteroskedasticity
14. White robust variance estimator. Explain why it works (under suitable assumptions).
15. The IV estimator when there are more instruments than regressors and the special case when the number of instruments is equal to the number of regressors.
16. Explain why the IV-estimator is consistent (and list the assumptions) but not unbiased. (Note: there isn't so much to remember about the assumptions, we basically assume "what we need" in order to get consistency.)
17. Maximum Likelihood.
  - (a) Be able to show that  $\hat{\beta}_{OLS} = \hat{\beta}_{ML}$  under the standard assumptions plus normality and explain the relation between the standard OLS estimate of the error variance and the ML estimate of the error variance.
  - (b) Also, be able to derive the (Normal) ML estimator in the case of heteroskedasticity. (I won't ask for the case of autocorrelated residuals.)
  - (c) Know the Cramer-Rao lower bound—in particular, that the inverse information matrix is the asymptotic variance of the estimator.
  - (d) Be able to prove the information matrix equality (maybe for a particular simple likelihood function).
  - (e) Be able to find the ML estimator for simple distributions such as exponential, log-normal, Bernoulli.