

Midterm Exam 1, March 9—3 questions. All sub-questions carry equal weight except where otherwise indicated.

1. (25%) a) State precisely the assumptions underlying Hall's 1978 Permanent Income Hypothesis/Model Model (PIH).
b) Derive the result that consumption is a martingale under these assumptions.

2. (25%) Assume a consumer maximizes the utility of consumption of N goods C_1, \dots, C_N using the utility index $U(C_1, \dots, C_N) = (\sum_{i=1}^N C_i^{\frac{\eta-1}{\eta}})^{\frac{\eta}{\eta-1}}$. The price of good i is P_i and the consumer faces the budget constraint $\sum_{i=1}^N P_i C_i = Y$ where Y is the consumer's exogenous income. (You can use an integral, rather than a sum, if you find it convenient.)

One can find that $C = Y/P$ for a price index P , where $C = (\sum_{i=1}^N C_i^{\frac{\eta-1}{\eta}})^{\frac{\eta}{\eta-1}}$. Derive P such that $C = Y/P$. Also find the optimal C_i in terms of P_i, P , and Y . (You will get 10 points for stating the right formula for P).

3. (50%) Assume that a time series z_t follows the Moving Average process

$$z_t = 10 + u_t + .8u_{t-1} + .7u_{t-2} .$$

- a) Find $\frac{\partial z_{t+1}}{\partial u_t}$.
b) Plot the Impulse Response Function (IRF) for z_t .

Now assume that income of an individual follows the process

$$y_t = 10 + .5y_{t-1} + u_t .$$

- c) Plot the IRF for y_t .

Next assume that you know that $y_0 = 0$.

- d) Find $E_0 y_1$ and $E_0 y_2$.

Now assume that the rate of interest is fixed and equal to 10 percent.

- e) Find the expected present value of present and future income; i.e., $(E_0 \sum_{t=0}^{\infty} (1+r)^{-t} y_t)$. [Hint: To get full point you need to solve for a compact expression; i.e., not give the answer as an infinite sum.]

Finally, assume the individual has no assets and his or her consumption follows the PIH model.

- f) What is c_0 , the individual's level of consumption in period 0?