ECONOMICS 7344, Spring 2005 Bent E. Sørensen March 22, 2005

## HOMEWORK 7. Due Monday March 28.

- 1. (7% of second core exam 2003.) Asset A and asset B exist for one period and their returns have identical covariances with the market return. The rate return of asset B has a variance that is twice as large as the variance of the rate of return of asset A. Which asset will—if the CAPM holds—have the highest expected rate of return?
- 2. Assume that the return on the market  $(R_M)$  is 10% and that a safe asset exists with a return of 6%. Assume that the standard CAPM is true.
- a) Let X is an asset whose payout is determined by you flipping a coin and paying 1\$ each heads and nothing if tails. What is the return  $(R_X)$  to an investment in X?
- b) Now let the return  $(R_i)$  to an asset be  $.5 * R_M + .5R_X$ . What is the expected value  $E(R_i)$ .
- c) If the asset X now paid out 100\$, rather than just 1\$, in the case of heads, and still nothing in the case of tails. What would now be the answer to b)?
- 3. Assume that IBM stock has a mean return of 3% and a variance of 4, and that GM stock has a mean return of 8% and a variance of 9. Also assume that the covariance between IBM and GM stock is 1. Calculate the mean and standard deviation for portfolios that consist of IBM and GM stocks: do this for 0, 25%, 50%, 75%, and 100% invested in IBM. Sketch (by hand) the efficient frontier when these are the only assets available.
- 4. Romer 7.3. [This is also based on a famous paper.]