# Credit Constraints and Growth in a Global Economy

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### Roadmap

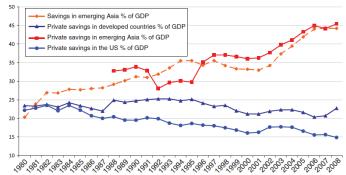
- Motivation and Contribution of the paper
- Summarize the paper
  - Theoretical framework and Mechanism
  - Empirical results
- Extension Ideas on the third year paper

### 1. Motivation and Contribution

- Three prominent global patterns:
  - 1. A divergence in savings rates
  - 2. Capital Outflows from emerging market economies
  - 3. A fall in the world interest rate
- The existing open-economy growth models do not explain this trend

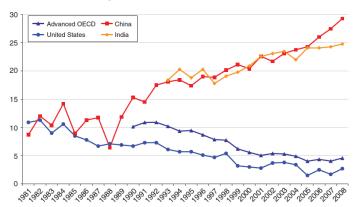
### 1. Motivation and Contribution





### 1. Motivation and Contribution

Panel B. Household saving rates



### 2. Theory

- Large Open Economies
- Overlapping Generations of consumers who live for three periods.  $\gamma \in \{y, m, o\}$
- People work when  $\gamma = y$  and  $\gamma = m$ . Consume only when  $\gamma = o$ .

#### 2.1 Production

Gross Output:

$$Y_t^i = \left(K_t^i\right)^{\alpha} \left[A_t^i \left(e_t^i L_{y,t}^i + L_{m,t}^i\right)\right]^{1-\alpha} \tag{1}$$

i: country index, t: time index  $K_t^i$ : aggregate capital stock  $e_t^i L_{y,t}^i + L_{m,t}^i$ : total labor input  $e_t^i$  (< 1): relative productivity of young worker  $A_t^i$ : country-specific productivity

#### 2.1 Production

#### Firm's First Order Conditions

- Wage:  $\omega_{y,t}^i = e_t^i (1-\alpha) A_t^i (k_t^i)^{\alpha}$ ,  $\omega_{m,t}^i = (1-\alpha) A_t^i (k_t^i)^{\alpha}$
- Rental Rate:  $r_{K,t}^i = \alpha(k_t^i)^{\alpha-1}$
- ullet Gross Rate of Return:  $R_t^i=1-\delta+r_{\mathcal{K},t}^i$
- $A_t^i = (1 + g_{A,t}^i)A_{t-1}^i$
- $L_{y,t}^i = (1 + g_{L,t}^i) L_{y,t-1}^i$



Lifetime Utility:

$$U_t^i = u(c_{y,t}^i) + \beta u(c_{m,t+1}^i) + \beta^2 u(c_{o,t+2}^i)$$

$$u(c) = (c^{1-\frac{1}{\sigma}} - 1)/(1 - \frac{1}{\sigma})$$
(2)

**Budget Constraints:** 

$$c_{y,t}^{i} + a_{y,t+1}^{i} = \omega_{y,t}^{i}$$
 (3)

$$c_{m,t+1}^{i} + a_{m,t+2}^{i} = \omega_{m,t+1}^{i} + R_{t+1}^{i} a_{y,t+1}^{i}$$
 (4)

$$c_{o,t+2}^{i} = R_{t+2}^{i} a_{m,t+2}^{i} \tag{5}$$



Young Agent's Credit Constraints:

$$a_{y,t+1}^{i} \ge -\theta^{i} \frac{\omega_{m,t+1}^{i}}{R_{t+1}^{i}}$$
 (6)

### Assumption1

Credit constraints for the young are binding at all times in all countries

- $\bullet$   $\theta^i$  is small enough
- the wage profile is steep enough

The net asset position of the young:

$$a_{y,t+1}^{i} = -\theta^{i} \frac{\omega_{m,t+1}^{i}}{R_{t+1}^{i}}$$
 (7)

The net asset position of a middle-aged agent:

$$a_{m,t+1}^{i} = \frac{1}{1 + \beta^{-\sigma}(R_{t+1}^{i})^{1-\sigma}} (1 - \theta^{i}) \omega_{m,t}^{i}$$
 (8)

# 2.3 Autarky Equilibrium

Market clearing:

$$K_{t+1}^{i} = L_{y,t}^{i} a_{y,t+1}^{i} + L_{m,t}^{i} a_{m,t+1}^{i}$$
(9)

Law of motion for  $k^i$ :

$$(1 + g_{A,t+1}^{i})(1 + g_{yL,t}^{i}) \left[ 1 + e_{t+1}^{i}(1 + g_{L,t+1}^{i}) + \theta^{i} \frac{1-\alpha}{\alpha} \right] k_{t+1}^{i}$$

$$= \frac{(1 - \theta^{i})(1 - \alpha)}{1 + \beta^{-\sigma} \left[ \alpha (k_{t+1}^{i})^{\alpha - 1} \right]^{1-\sigma}} (k_{t}^{i})^{\alpha}$$
 (10)

### 2.3 Autarky Equilibrium

#### Theorem 1

Suppose that  $\delta=1$ . There exists a unique, stable, autarky steady state. All else equal more constrained economies have a higher capital-to-efficient labor ratio  $(dk^i/d\theta^i<0)$  and a lower interest rate  $(dR^i/d\theta^i>0)$ .

US: less-constrained economy, China: more-constrained economy  $\Rightarrow \theta^{US} = \theta_H$  and  $\theta^{China} = \theta_L$ 

- $\theta^{US} > \theta^{China}$
- $(k^*)^{US} < (k^*)^{China}$
- $(R^*)^{US} > (R^*)^{China}$

### 2.4 Integrated Equilibrium

Financial Integration: 
$$R_{t+1}^i = R_{t+1}$$
 and  $k_{t+1}^i = k_{t+1}$ 

The capital market equilibrium condition:

$$\sum_{i} K_{t+1}^{i} = \sum_{i} (L_{y,t}^{i} a_{y,t+1}^{i} + L_{m,t}^{i} a_{m,t+1}^{i})$$
 (11)

### 2.4 Integrated Equilibrium

### Proposition 1

Suppose that  $\delta = 1$ . Let  $\theta_L \equiv \min_i \{\theta^i\}$ ,  $\theta_H \equiv \max_i \{\theta^i\}$ , with  $\theta_L \neq \theta_H$ . The steady state world interest rate R satisfies

$$R(\theta_L) < R < R(\theta_H) \tag{12}$$

where  $R(\theta)$  denotes the autarky steady state rate for credit constraint parameter  $\theta$ .

### 2.3 Autarky Equilibrium

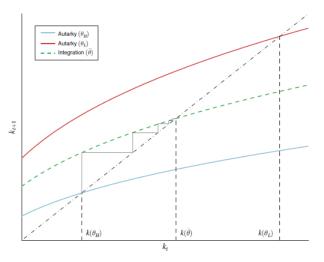


FIGURE 3. LAW OF MOTION AND STEADY STATE: AUTARKY AND INTEGRATION

Notes: Parameter values are  $\sigma = 0.5$ ,  $\beta = 0.97$  (annual),  $\alpha = 0.28$ ,  $\delta = 10$  percent (annual),  $\theta_H = 0.2$ ,  $\theta_L = 0.02$ ,  $g_A = 1.5$  percent (annual),  $g_L = 1$  percent, e = 0.33. A period lasts 20 years.

### 2.4 Integrated Equilibrium

What causes a fall in the world interest rate R

• Financial integration

Credit constraint: 
$$\bar{\theta} \equiv \sum_{i} \lambda^{i} \theta^{i}$$
 where  $\lambda^{i} \equiv \frac{A_{i,t}(eL_{y,t}^{i} + L_{m,t}^{i})}{\sum_{j} A_{i,t}(eL_{y,t}^{i} + L_{m,t}^{i})}$ 

• A relative expansion of a more constrained economies (ex. China)

### 2.4 Integrated Equilibrium

### Proposition 2

A relative expansion of the more constrained economies (i.e., an increase in the share with  $\lambda^i$  of a country with low  $\theta^i$ ) causes a fall in the world interest rate. A relative expansion of less constrained economies has the opposite effect.

# 2.5 Saving and Investment

	China (θ <sub>L</sub> )	U.S.(θ <sub>H</sub> )
Young	saving ↓	saving ↓↓
Middle-aged	saving ↑↑	Saving ↑

A fall in R 
$$\Rightarrow$$
  $S_{China} \uparrow$  and  $S_{US} \downarrow$ 

Asymmetric credit constraints (across countries and generations)

 $\Rightarrow$  Heterogeneous responses of savings rates

# 2.5 Saving and Investment

### Proposition 3

In an integrated global economy with heterogenous credit constraints, a fall in the world rate of return induces a greater dispersion in saving rates across countries

### 3. Empirical Results

- U.S. Consumer Expenditure Survey (1986-2008) and National Income and Product Account (NIPA)
- China: Urban Household Survey (1986, 1992-2009)

- Young's (under 25) saving rate over time is markedly different (US: 12.7% decline in savings + China: Savings rises little)
- Savings rate of the middle-aged (35-54) rose by about 15 percentage more in China than in the U.S. (US: 2.3% increase)

#### 4. Conclusion

- Three-period Overlapping Generations type Households' consumption-saving decision with heterogeneous credit constraints
- Mechanism to explain a fall in the world interest rate as well as divergence in saving rates and capital outflows from developing countries
- Consistent with data and global patterns

### 5. Extension

#### Ideas on the third year paper:

The effects of decline in trade costs on the trade imbalances under the existence of credit constraints

- Static component: Eaton-Kortum (2002) + Endogenous capital
- Dynamic component: CGJ paper (Three-period OLG type Households' consumption-saving decision)

### 5. Extension: Household's problem

#### Household's Max problem

$$U_t^i = \phi_y u(c_{i,y,t}) + \beta \phi_m u(c_{i,m,t+1}) + \beta^2 \phi_o u(c_{i,o,t+2})$$
 (13)

$$P_{i,t}c_{i,y,t} + a_{i,y,t+1} = w_{i,y,t}$$
 (14)

$$P_{i,t+1}c_{i,m,t+1} + c_{i,m,t+2} = w_{i,m,t+1} + R_{i,t+1}a_{i,y,t+1}$$
 (15)

$$P_{i,t+2}c_{i,o,t+2} + c_{i,m,t+2} = R_{i,t+2}a_{i,m,t+2}$$
(16)

### 5. Extension: Household's problem

Euler equations:

$$(c_{i,y,t})^{-\rho} = \beta \frac{\phi_m}{\phi_v} \frac{R_{i,t+1} P_{i,t}}{P_{i,t+1}} (c_{i,m,t+1})^{-\rho}$$
(17)

$$(c_{i,m,t+1})^{-\rho} = \beta \frac{\phi_o}{\phi_m} \frac{R_{i,t+2} P_{i,t+1}}{P_{i,t+2}} (c_{i,o,t+2})^{-\rho}$$
(18)

### 5. Extension

#### Why? Expected Results?

- Household's consumption-saving decision is influenced by 'credit constraints'
- Compare to frictionless market case:
   Over-estimation vs Under-estimation

# Thank you