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## ECONOMICS 7330-Probability and Statistics, Fall 2022

Homework 1. Monday August 22. Due Wednesday August 31.

1. Let $A=a, b, c, d$ and $B=a, c, e, f$.
(a) Find $A \cup B$.
(b) Find $A \cap B$.
2. Describe the sample space $S$ for the following experiments.
(a) Flip a coin.
(b) Roll a six-sided die.
(c) Roll two six-sided dice.
3. Prove that $P[A \cup B]=P[A]+P[B]-P[A \cap B]$.

4 Show that $P[A \cap B] \leq P[A] \leq P[A \cup B] \leq P[A]+P[B]$.
5. Prove that $\left[\bigcup_{i=1}^{\infty} A_{i}\right]^{C}=\bigcap_{i=1}^{\infty} A_{i}^{C}$.
6. We observe the price of 2 stocks, stock A and stock B.

The probability that the price of stock A increases is 0.8 and the probability that the price of stock B increases is 0.5 . We also know that the probability of the event that the price of either stock A or stock B increases is 0.9.
a) What is the probability that the price of stock A increases at the same time as the price of stock B increases?
b) What is the probability that the price of A increases if you observe that the price of stock B increases?
(State clearly which formulas you used).

